

第一次作业参考答案

习题一

1.(2) $S = \{2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$

(3) $s = \{x \in N | x \geq 1\}$

(5) $s = \{x \in R | x \geq 0\}$

4. $B_1 = \{A_6, A_4A_5, A_1A_3, A_1A_2\}$

$B_2 = \{A_1A_6, A_1A_2A_5, A_1A_2A_3A_4\}$

5.解： 利用公式

$$A - B = A - AB = A\bar{B}$$

$$A + B = A + (B - A) = A + (B - AB) = A + B\bar{A}$$

或

$$A + B = (A - AB) + AB + (B - AB)$$

于是

$$A + B + C = A + (B + C) = A + (B + C)\bar{A}$$

$$= A + (B + C\bar{B})\bar{A} = A + B\bar{A} + C\bar{B}\bar{A}$$

$$= A + (B - AB) + [C - (A + B)C]$$

6.(1) $P(A) = \frac{2}{5} \times \frac{2}{5} = \frac{4}{25}$

“至少取到一个正品”的对立事件为“取到两个均为次品”，所以 $P(B) = 1 - P(A)$.

$$P(B) = 1 - P(A) = 1 - \frac{4}{25} = \frac{21}{25}$$

(2) $P(A) = \frac{2}{5} \times \frac{1}{4} = \frac{1}{10}$

$$P(B) = 1 - P(A) = 1 - \frac{1}{10} = \frac{9}{10}$$

(3) $P(A) = \frac{C_2^2}{C_5^2} = \frac{1}{10}$

$$P(B) = 1 - P(A) = 1 - \frac{1}{10} = \frac{9}{10}$$

8. 记“点数相同”为事件A,“同花”为事件B, 则

$$\langle \text{法一} \rangle P(A) = \frac{13 \times C_4^2}{C_{52}^2} = \frac{1}{17}$$

$$P(B) = \frac{4 \times C_{13}^2}{C_{52}^2} = \frac{4}{17}$$

$$\langle \text{法二} \rangle P(A) = \frac{52}{52} \times \frac{3}{51} = \frac{1}{17}$$

$$P(B) = \frac{52}{52} \times \frac{12}{51} = \frac{4}{17}$$